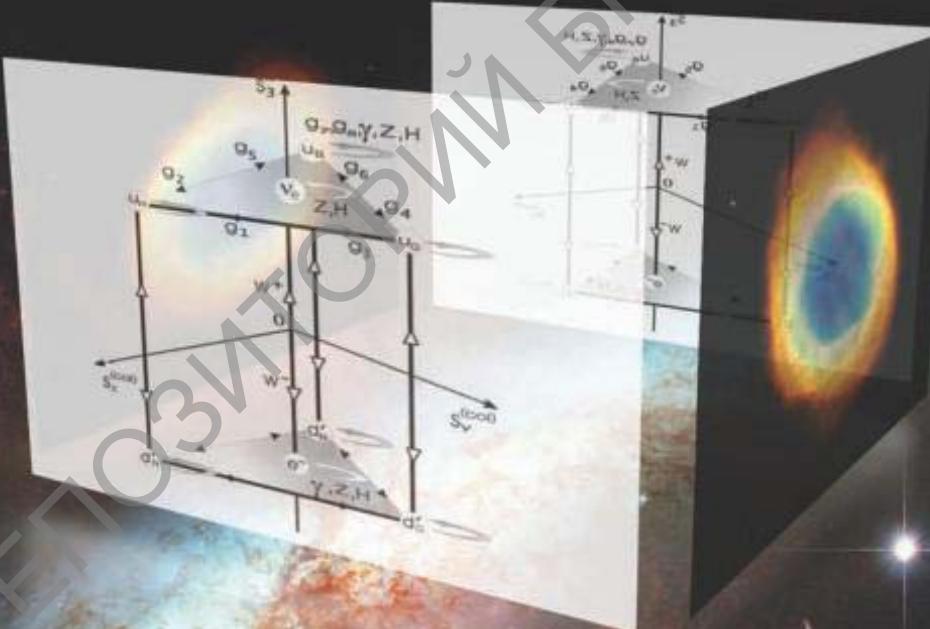


# Advanced Particle Physics

Volume II

## The Standard Model and Beyond



O. M. Boyarkin

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