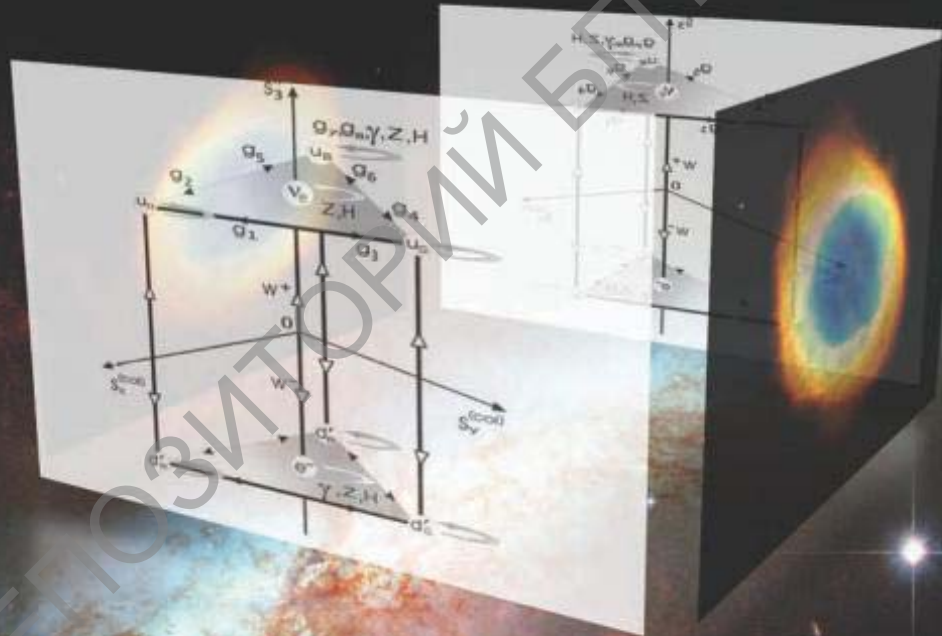


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Advanced Particle Physics

Volume I

Particles, Fields, and
Quantum Electrodynamics



O. M. Boyarkin

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